Motivation	Methodology 0000	Bias 0000	(Co)variability 00000	Correlation 0000	Conclusions

Real-time bias correction of an atmospheric general circulation model

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Is there a relationship between model "fidelity" and model "skill"?

- CCCma's AGCM3 (Scinocca et al. 2008)
- a method to construct real-time corrections to reduce model bias is introduced.
- two sets of AMIP-type ensemble simulations ("hindcasts") with and without bias-correcting terms are discussed.
- changes in model co-variability and skill on *seasonal* time scale are examined.



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Consider a dynamical model:

$$\frac{\partial X}{\partial t} = F(X)$$

where X represents the model state, F(X) is the model tendency (advection, physics, etc.) The goal is to find a r.h.s. term g

$$\frac{\partial X}{\partial t} = F(X) + g$$

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that reduces model bias $\overline{X} - \overline{X}_{obs}$.



 $\frac{\partial X}{\partial t} = F(X) + g$

DelSole et al. (2008), Yang et al (2008) refer to this approach as *"empirical correction"*.

- DelSole et al. (2008) consider several strategies for estimating *g*. The best strategy is based on 24-hr error tendencies.
- The forecast bias is generally reduced (except for U and V).
- None of the considered methods consistently improves skill (may be model dependent). Caveats: JJA only, short 10-yr runs.



Relaxation runs

Relaxation runs: 5-member ensemble AMIP-type runs with AGCM3 by relaxing model solution to ERA interim reanalysis:

$$\frac{\partial X}{\partial t} = F(X) - \frac{1}{\tau}(X - X_R)$$

where X_R is ERA interim reanalysis.

• VORT, DIV, TEMP, and SHUM are relaxed.

• τ =36hrs for VORT, DIV, TEMP, and τ =72hrs for SHUM. (for τ =24–36hrs, $|X - X_R| \approx |X_{R1} - X_{R2}|$)

 Only larger scales are relaxed with full strength (T1-T21). (Gaussian filter for T22-T63 with half-decay at ≈T35).

• Weaker relaxation near the model top above ${\approx}100\mathrm{hPa}.$ Empirical bias correction:

$$g = -\frac{\overline{(X - X_R)}^{AC}}{\tau}$$



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• *Control* runs: 10-member ensemble of AMIP runs with AGCM3 for years 1959-2008:

$$\frac{\partial X}{\partial t} = F(X)$$

• *Bias-corrected* runs: 10-member ensemble of AMIP runs with AGCM3 by adding the climatological tendency term *g*:

$$\frac{\partial X}{\partial t} = F(X) + g$$



Z500 bias vs ERA interim, 1989-2008

CONTROL

AVG=-13.3M RMS=29.6M

BIAS-CORRECTED

AVG= -5.6M RMS=17.1M



AVG=-12.5M RMS=32.9M



AVG=-11.1M RMS=19.4M





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Motivation	Methodology 0000	Bias ○○○●	(Co)variability 00000	Correlation 0000	Conclusions
Conclusio	n 1				

The model climatology is improved.



Multivariate normal distribution

Variability distribution on monthly to seasonal time scales is assumed to be multivariate normal:



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 Kullback-Leibler (KL)
 divergence

Kullback-Leibler divergence (also information divergence, information gain, or relative entropy) is a non-symmetric measure of the difference between two probability distributions P and Q.

$$D_{\mathsf{KL}}(P \| Q) = \int p(x) \log \frac{p(x)}{q(x)} dx$$

Typically P represents the "true" distribution of data, or observations. Q typically represents a model distribution.

For two multivariate normal distributions $N_p(\Sigma_p)$ and $N_q(\Sigma_q)$:

$$D_{\mathsf{KL}}(N_{\rho} \| N_{q}) = \frac{1}{2} \left(\log_{e} \left(\frac{\det \Sigma_{q}}{\det \Sigma_{\rho}} \right) + \operatorname{tr} \left(\Sigma_{q}^{-1} \Sigma_{\rho} \right) - N \right)$$

where Σ_q and Σ_q are the auto-covariance matrices.

Motivation Methodology Bias (Co)variability Correlation Conclusions Kullback-Leibler (KL) divergence

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Motivation	Methodology 0000	Bias 0000	(Co)variability ○○○○●	Correlation 0000	Conclusions
Conclusio	n 2				

Interannual co-variability is generally improved.





Correlation, Z500, 1959-2008



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Correlation, Z1000, 1959-2008



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Correlation, T850, 1959-2008



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Motivation	Methodology 0000	Bias 0000	(Co)variability 00000	Correlation 0000	Conclusions
Conclusio	on 3				

Skill of seasonal "hindcasts" is modestly improved.



- The presented method reduces climatological biases in AGCM3.
- Interannual atmospheric co-variability is generally improved.
- Potential skill of seasonal hindcasts is modestly improved.

It isn't unreasonable to expect that models with smaller bias produce more skillful seasonal predictions.

Outlook:

- Are results reproducible in AGCM4?
- Can a similar approach be implemented in a coupled model?
 - run-time bias-correcting tendencies are not conservative.

• how to bias-correct OGCM?



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• how to bias-correct OGCM?